

Problem A-one

From good old QED:

$$e \begin{pmatrix} \langle B | \\ \langle B | \end{pmatrix}^T \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} \sigma_r \\ \bar{\sigma}_r \end{pmatrix} \begin{pmatrix} |A\rangle \\ |A\rangle \end{pmatrix} \frac{\langle \xi | \sigma_r | \eta \rangle}{\sqrt{2} \langle \xi \eta \rangle} \quad (2\pi)^4 \delta^4(p_A - p_B) \quad (a)$$

$$\left(\frac{e \delta^4}{\sqrt{2} \langle \xi \eta \rangle} \right) \left(\langle B \eta | \langle \xi A \rangle + \langle B \xi | \langle \eta A \rangle \right) \quad (b)$$

$$= \frac{1}{\langle \eta \hat{P}_A \xi \rangle} \left(\langle B \eta | \langle \eta \hat{P}_A \xi | \langle \xi A \rangle + \langle B \xi | \langle \xi \bar{P}_A \eta | \langle \eta A \rangle \right)$$

$$(c) \quad |\eta \rangle \langle \eta | = \hat{1}$$

$$= \left(\langle B \bar{\eta} \hat{P}_A \xi | A \rangle + \langle B \hat{\xi} \bar{P}_A \hat{\eta} | A \rangle \right)$$

$$= \left(- \langle B \bar{P}_A \hat{\eta} \hat{\xi} | A \rangle - \langle B \hat{\xi} \bar{\eta} \hat{P}_A | A \rangle \right) \quad (c)$$

$$= \left(- \langle A \hat{\xi} \bar{\eta} \hat{P}_A | B \rangle \right) \quad "$$

$$= \left(\langle A \hat{\xi} \bar{\eta} (\hat{1} + \beta_B) | B \rangle \right)$$

$$= \left(m \langle A \hat{\xi} \bar{\eta} | B \rangle - \langle B \hat{\xi} \bar{\eta} | A \rangle m \right) \quad (d)$$

$$\frac{e}{\sqrt{2} \langle \eta \hat{P}_A \xi | \xi \eta \rangle} \left(m \langle A (\hat{\xi} \bar{\eta} + \hat{\eta} \hat{\xi}) | B \rangle \right)$$

(c)

$$\frac{e}{\sqrt{2}} \frac{m \langle \xi \eta \rangle [\eta \xi]}{\langle \eta \hat{p}_A \xi \rangle \langle \xi \eta \rangle} \langle AB \rangle$$

(Dirac delta)

Solution